

2025 AMC 12A

Try this exam as a timed Mock Exam on the

ZIML Practice Page (click here)

View answers and concepts tested in our

2025 AMC 10A+12A Blog Post (click here)

The problems in the AMC-Series Contests are copyrighted by American Mathematics Competitions at Mathematical Association of America (www.maa.org).



Question 1

Not yet answered

Points out of 6

Andy and Betsy both live in Mathville. Andy leaves Mathville on his bicycle at $1:30$, traveling due north at a steady 8 miles per hour. Betsy leaves on her bicycle from the same point at $2:30$, traveling due east at a steady 12 miles per hour. At what time will they be exactly the same distance from their common starting point?

$\textbf{(A)}\ 3{:}30 \qquad \textbf{(B)}\ 3{:}45 \qquad \textbf{(C)}\ 4{:}00 \qquad \textbf{(D)}\ 4{:}15 \qquad \textbf{(E)}\ 4{:}30$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 2

Not yet answered

Points out of 6

A box contains 10 pounds of a nut mix that is 50 percent peanuts, 20 percent cashews, and 30 percent almonds. A second nut mix containing 20 percent peanuts, 40 percent cashews, and 40 percent almonds is added to the box resulting in a new nut mix that is 40 percent peanuts. How many pounds of cashews are now in the box?

$\textbf{(A)}\ 3.5 \qquad \textbf{(B)}\ 4 \qquad \textbf{(C)}\ 4.5 \qquad \textbf{(D)}\ 5 \qquad \textbf{(E)}\ 6$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 3

Not yet answered

Points out of 6

A team of students is going to compete against a team of teachers in a trivia contest. The total number of students and teachers is 15. Ash, a cousin of one of the students, wants to join the contest. If Ash plays with the students, the average age on that team will increase from 12 to 14. If Ash plays with the teachers, the average age on that team will decrease from 55 to 52. How old is Ash?

$\textbf{(A)}\ 28 \qquad \textbf{(B)}\ 29 \qquad \textbf{(C)}\ 30 \qquad \textbf{(D)}\ 32 \qquad \textbf{(E)}\ 33$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 4

Not yet answered

Points out of 6

Agnes writes the following four statements on a blank piece of paper.

- At least one of these statements is true.
- At least two of these statements are true.
- At least two of these statements are false.
- At least one of these statements is false.

Each statement is either true or false. How many false statements did Agnes write on the paper?

$\textbf{(A)}\ 0 \qquad \textbf{(B)}\ 1 \qquad \textbf{(C)}\ 2 \qquad \textbf{(D)}\ 3 \qquad \textbf{(E)}\ 4$

Select one:

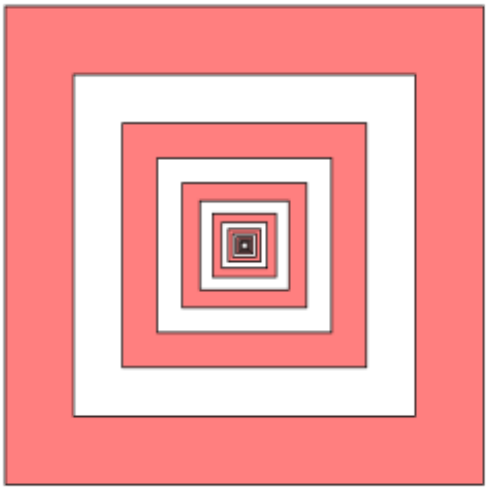
- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 5

Not yet answered

Points out of 6

In the figure below, the outside square contains infinitely many squares, each of them with the same center and sides parallel to the outside square. The ratio of the side length of a square to the side length of the next inner square is k, where $0 < k < 1$. The spaces between squares are alternately shaded, as shown in the figure (which is not necessarily drawn to scale).



The area of the shaded portion of the figure is 64% of the area of the original square. What is k?

$\textbf{(A)}\ \frac{3}{5} \qquad \textbf{(B)}\ \frac{16}{25} \qquad \textbf{(C)}\ \frac{2}{3} \qquad \textbf{(D)}\ \frac{3}{4} \qquad \textbf{(E)}\ \frac{4}{5}$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 6

Not yet answered

Points out of 6

Six chairs are arranged around a round table. Two students and two teachers randomly select four of the chairs to sit in. What is the probability that the two students will sit in two adjacent chairs and the two teachers will also sit in two adjacent chairs?

$\textbf{(A)}\ \frac{1}{6} \qquad \textbf{(B)}\ \frac{1}{5} \qquad \textbf{(C)}\ \frac{2}{9} \qquad \textbf{(D)}\ \frac{3}{13} \qquad \textbf{(E)}\ \frac{1}{4}$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 7

Not yet answered

Points out of 6

In a certain alien world, the maximum running speed v of an organism is dependent on its number of toes n and number of eyes m. The relationship can be expressed as $v = kn^a m^b$ centimeters per hour, where k, a, b are integer constants. In a population where all organisms have 5 toes, $\log v = 4 + 2\log m$; and in a population where all organisms have 25 eyes, $\log v = 4 + 4\log n$, where all logs are in base 10. What is $k + a + b$?

$\textbf{(A)}\ 20 \qquad \textbf{(B)}\ 21 \qquad \textbf{(C)}\ 22 \qquad \textbf{(D)}\ 23 \qquad \textbf{(E)}\ 24$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 8

Not yet answered

Points out of 6

Pentagon $ABCDE$ is inscribed in a circle, and $\angle BEC = \angle CED = 30^\circ$. Let line AC and line BD intersect at point F, and suppose that $AB = 9$ and $AD = 24$. What is BF?

$\textbf{(A)}\ \frac{57}{11} \qquad \textbf{(B)}\ \frac{59}{11} \qquad \textbf{(C)}\ \frac{60}{11} \qquad \textbf{(D)}\ \frac{61}{11} \qquad \textbf{(E)}\ \frac{63}{11}$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 9

Not yet answered

Points out of 6

Let w be the complex number $2 + i$, where $i = \sqrt{-1}$. What real number r has the property that r, w, and w^2 are three collinear points in the complex plane?

$\textbf{(A)}\ \frac{3}{4} \qquad \textbf{(B)}\ 1 \qquad \textbf{(C)}\ \frac{7}{5} \qquad \textbf{(D)}\ \frac{3}{2} \qquad \textbf{(E)}\ \frac{5}{3}$

Select one:

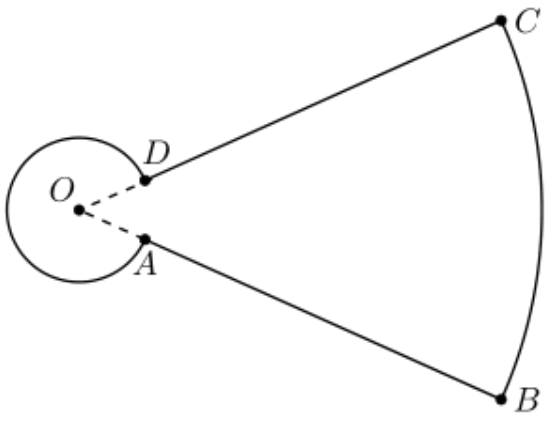
- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 10

Not yet answered

Points out of 6

In the figure shown below, major arc $\widehat{AD}$ and minor arc $\widehat{BC}$ have the same center, O. Also, A lies between O and B, and D lies between O and C. Major arc $\widehat{AD}$, minor arc $\widehat{BC}$, and each of the two segments $\overline{AB}$ and $\overline{CD}$ have length 2π. What is the distance from O to A?



(A) 1 **(B)** $1-\pi+\sqrt{\pi^2+1}$ **(C)** $\frac{\pi}{2}$ **(D)** $\frac{\sqrt{\pi^2+1}}{2}$ **(E)** 2

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 11

Not yet answered

Points out of 6

The orthocenter of a triangle is the concurrent intersection of the three (possibly extended) altitudes. What is the sum of the coordinates of the orthocenter of the triangle whose vertices are $A(2,31)$, $B(8,27)$, and $C(18,27)$?

(A) 5 **(B)** 17 **(C)** $10+4\sqrt{17}+2\sqrt{13}$ **(D)** $\frac{113}{3}$ **(E)** 54

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 12

Not yet answered

Points out of 6

The *harmonic mean* of a collection of numbers is the reciprocal of the arithmetic mean of the reciprocals of the numbers in the collection. For example, the harmonic mean of $4, 4$, and 5 is

$$\frac{1}{\frac{1}{3}(\frac{1}{4}+\frac{1}{4}+\frac{1}{5})} = \frac{30}{7}.$$

What is the harmonic mean of all the real roots of the 4050th degree polynomial

$$\prod_{k=1}^{2025}(kx^2-4x-3) = (x^2-4x-3)(2x^2-4x-3)(3x^2-4x-3)\ldots(2025x^2-4x-3)?$$

$\textbf{(A)}\ -\frac{5}{3}$ $\textbf{(B)}\ -\frac{3}{2}$ $\textbf{(C)}\ -\frac{6}{5}$ $\textbf{(D)}\ -\frac{5}{6}$ $\textbf{(E)}\ -\frac{2}{3}$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 13

Not yet answered

Points out of 6

Let $C = \{1, 2, 3, \ldots, 13\}$. Let N be the greatest integer such that there exists a subset of C with N elements that does not contain five consecutive integers. Suppose N integers are chosen at random from C without replacement. What is the probability that the chosen elements do not include five consecutive integers?

$\textbf{(A)}\ \frac{3}{130}$ $\textbf{(B)}\ \frac{3}{143}$ $\textbf{(C)}\ \frac{5}{143}$ $\textbf{(D)}\ \frac{1}{26}$ $\textbf{(E)}\ \frac{5}{78}$

Select one:

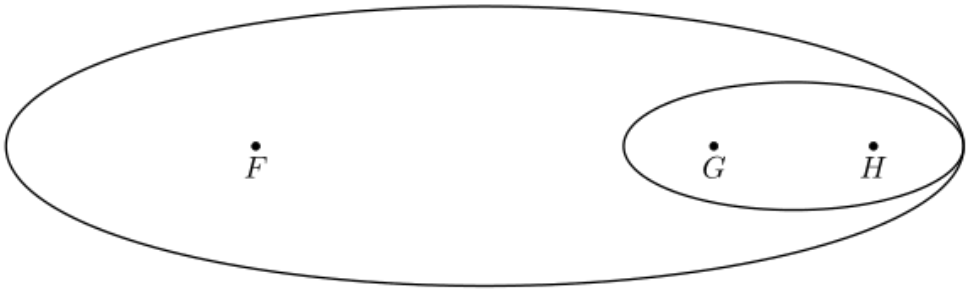
- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 14

Not yet answered

Points out of 6

Points F, G, and H are collinear with G between F and H. The ellipse with foci at G and H is internally tangent to the ellipse with foci at F and G, as shown below.



The two ellipses have the same eccentricity e, and the ratio of their areas is 2025. (Recall that the eccentricity of an ellipse is $e = \frac{c}{a}$, where c is the distance from the center to a focus, and $2a$ is the length of the major axis.) What is e?

$\textbf{(A)}\ \frac{3}{5}$ $\textbf{(B)}\ \frac{16}{25}$ $\textbf{(C)}\ \frac{4}{5}$ $\textbf{(D)}\ \frac{22}{23}$ $\textbf{(E)}\ \frac{44}{45}$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 15

Not yet answered

Points out of 6

A set of numbers is called *sum-free* if whenever x and y are (not necessarily distinct) elements of the set, $x + y$ is not an element of the set. For example, $\{1, 4, 6\}$ and the empty set are sum-free, but $\{1, 4, 5\}$ is not. What is the greatest possible number of elements in a sum-free subset of $\{1, 2, 3, \ldots, 20\}$?

$\textbf{(A)}\ 8$ $\textbf{(B)}\ 9$ $\textbf{(C)}\ 10$ $\textbf{(D)}\ 11$ $\textbf{(E)}\ 12$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 16

Not yet answered

Points out of 6

Triangle $\triangle ABC$ has side lengths $AB = 80$, $BC = 45$, and $AC = 75$. The bisector of $\angle B$ and the altitude to side $\overline{AB}$ intersect at point P. What is BP?

$\textbf{(A)}\ 18 \qquad \textbf{(B)}\ 19 \qquad \textbf{(C)}\ 20 \qquad \textbf{(D)}\ 21 \qquad \textbf{(E)}\ 22$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 17

Not yet answered

Points out of 6

The polynomial $(z+i)(z+2i)(z+3i)+10$ has three roots in the complex plane, where $i = \sqrt{-1}$. What is the area of the triangle formed by these three roots?

$\textbf{(A)}\ 6 \qquad \textbf{(B)}\ 8 \qquad \textbf{(C)}\ 10 \qquad \textbf{(D)}\ 12 \qquad \textbf{(E)}\ 14$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 18

Not yet answered

Points out of 6

How many ordered triples (x, y, z) of different positive integers less than or equal to 8 satisfy $xy > z$, $xz > y$, and $yz > x$?

$\textbf{(A)}\ 36 \qquad \textbf{(B)}\ 84 \qquad \textbf{(C)}\ 186 \qquad \textbf{(D)}\ 336 \qquad \textbf{(E)}\ 486$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 19

Not yet answered

Points out of 6

Let a, b, and c be the roots of the polynomial $x^3 + kx + 1$. What is the sum

$$a^3b^2 + a^2b^3 + b^3c^2 + b^2c^3 + c^3a^2 + c^2a^3?$$

$\textbf{(A)}\ -k \qquad \textbf{(B)}\ -k+1 \qquad \textbf{(C)}\ 1 \qquad \textbf{(D)}\ k-1 \qquad \textbf{(E)}\ k$

Select one:

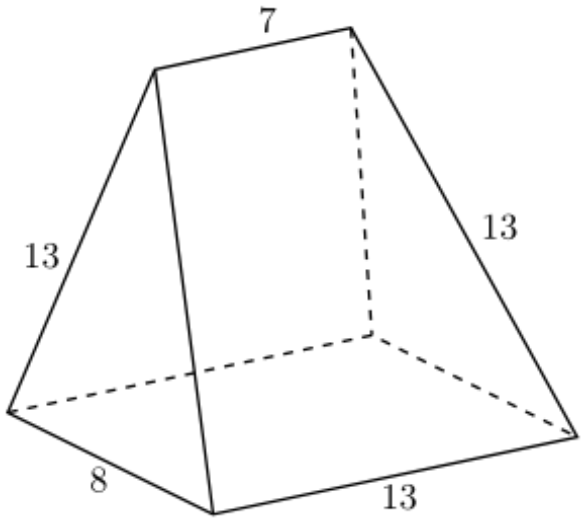
- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 20

Not yet answered

Points out of 6

The base of the pentahedron shown below is a 13×8 rectangle, and its lateral faces are two isosceles triangles with base of length 8 and congruent sides of length 13, and two isosceles trapezoids with bases of length 7 and 13 and nonparallel sides of length 13.



What is the volume of the pentahedron?

$\textbf{(A)}\ 416 \qquad \textbf{(B)}\ 520 \qquad \textbf{(C)}\ 528 \qquad \textbf{(D)}\ 676 \qquad \textbf{(E)}\ 832$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 21

Not yet answered

Points out of 6

There is a unique ordered triple (a, k, m) of nonnegative integers such that

$$\frac{4^a + 4^{a+k} + 4^{a+2k} + \cdots + 4^{a+mk}}{2^a + 2^{a+k} + 2^{a+2k} + \cdots + 2^{a+mk}} = 964.$$

What is $a + k + m$?

$\mathbf{(A)}\ 8 \qquad \mathbf{(B)}\ 9 \qquad \mathbf{(C)}10 \qquad \mathbf{(D)}\ 11 \qquad \mathbf{(E)}\ 12$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 22

Not yet answered

Points out of 6

Three real numbers are chosen independently and uniformly at random between 0 and 1. What is the probability that the greatest of these three numbers is greater than 2 times each of the other two numbers? (In other words, if the chosen numbers are $a \geq b \geq c$, then $a > 2b$.)

Three real numbers are chosen independently and uniformly at random between 0 and 1. What is the probability that the greatest of these three numbers is greater than the sum of the other two numbers?

$\mathbf{(A)}\ \frac{1}{12} \qquad \mathbf{(B)}\ \frac{1}{9} \qquad \mathbf{(C)}\ \frac{1}{8} \qquad \mathbf{(D)}\ \frac{1}{6} \qquad \mathbf{(E)}\ \frac{1}{4}$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 23

Not yet answered

Points out of 6

Call a positive integer fair if no digit is used more than once, it has no 0s, and no digit is adjacent to two greater digits. For example, $196, 23$ and 12463 are fair, but $1546, 320$, and 34321 are not. How many fair positive integers are there?

$\textbf{(A)}\ 511 \qquad \textbf{(B)}\ 2584 \qquad \textbf{(C)}\ 9841 \qquad \textbf{(D)}\ 17711 \qquad \textbf{(E)}\ 19682$

Select one:

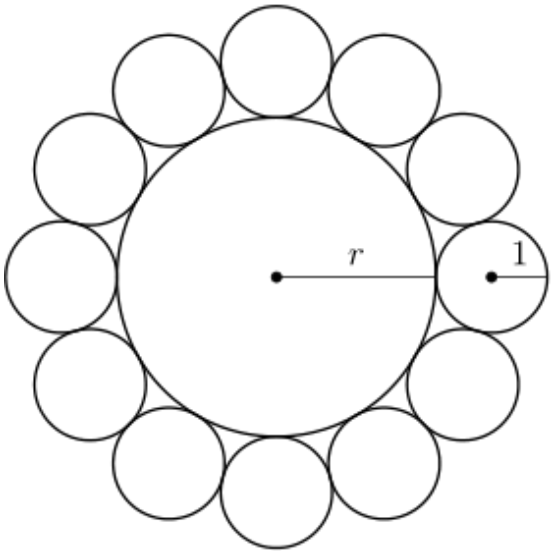
- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 24

Not yet answered

Points out of 6

A circle of radius r is surrounded by 12 circles of radius 1, externally tangent to the central circle and sequentially tangent to each other, as shown. Then r can be written as $\sqrt{a}+\sqrt{b}+c$, where a, b, c are integers. What is $a+b+c$?



$\textbf{(A)}\ 3 \qquad \textbf{(B)}\ 5 \qquad \textbf{(C)}\ 7 \qquad \textbf{(D)}\ 9 \qquad \textbf{(E)}\ 11$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**

Question 25

Not yet answered

Points out of 6

Polynomials $P(x)$ and $Q(x)$ each have degree 3 and leading coefficient 1, and their roots are all elements of $\{1, 2, 3, 4, 5\}$. The function $f(x) = \frac{P(x)}{Q(x)}$ has the property that there exist real numbers $a < b < c < d$ such that the set of all real numbers x such that $f(x) \leq 0$ consists of the closed interval $[a, b]$ together with the open interval (c, d). How many functions $f(x)$ are possible?

$\textbf{(A)}\ 7 \qquad \textbf{(B)}\ 9 \qquad \textbf{(C)}\ 11 \qquad \textbf{(D)}\ 12 \qquad \textbf{(E)}\ 13$

Select one:

- **A**
- **B**
- **C**
- **D**
- **E**
- **Leave blank (1.5 points)**